

The result of calling `repr` on a value is what Python displays in an interactive session

The result of calling `str` on a value is what Python prints using the `print` function

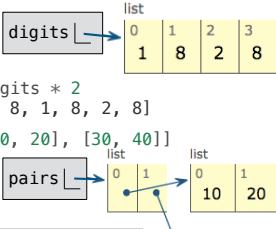
```
>>> today = datetime.date(2019, 10, 13)
>>> repr(today) # or today.__repr__()
'datetime.date(2019, 10, 13)'
>>> str(today) # or today.__str__()
'2019-10-13'
```

The result of evaluating an f-string literal contains the str string of the value of each sub-expression.

```
>>> f'pi starts with {pi}...'
'pi starts with 3.141592653589793...'
>>> print(f'pi starts with {pi}...')
pi starts with 3.141592653589793...
```

Lists:

```
>>> digits = [1, 8, 2, 8]
>>> len(digits)
4
>>> digits[3]
8
>>> [2, 7] + digits * 2
[2, 7, 1, 8, 2, 8, 1, 8, 2, 8]
>>> pairs = [[10, 20], [30, 40]]
>>> pairs[1]
[30, 40]
>>> pairs[1][0]
30
```



Executing a for statement:
for <name> in <expression>:
 <suite>

- Evaluate the header <expression>, which must yield an iterable value (a list, tuple, iterator, etc.)
- For each element in that sequence, in order:
 - Bind <name> to that element in the current frame
 - Execute the <suite>

Unpacking in a for statement: A sequence of fixed-length sequences

```
>>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
>>> same_count = 0
```

A name for each element in a fixed-length sequence

```
>>> for x, y in pairs:
...     if x == y:
...         same_count = same_count + 1
>>> same_count
2
```

..., -3, -2, -1, 0, 1, 2, 3, 4, ...

range(-2, 2)

Length: ending value - starting value
Element selection: starting value + index

```
>>> list(range(-2, 2))
[-2, -1, 0, 1]
```

List constructor

```
>>> list(range(4))
[0, 1, 2, 3]
```

Range with a 0 starting value

```
Membership:
>>> digits = [1, 8, 2, 8]
>>> 2 in digits
True
>>> 1828 not in digits
True

Slicing:
>>> digits[0:2]
[1, 8]
>>> digits[1:]
[8, 2, 8]
```

Slicing creates a new object

Identity:
<exp0> is <exp1>
evaluates to True if both <exp0> and <exp1> evaluate to the same object

Equality:
<exp0> == <exp1>
evaluates to True if both <exp0> and <exp1> evaluate to equal values
Identical objects are always equal values

List comprehensions:

```
[<map exp> for <name> in <iter exp> if <filter exp>]
Short version: [<map exp> for <name> in <iter exp>]
```

A combined expression that evaluates to a list using this evaluation procedure:

- Add a new frame with the current frame as its parent
- Create an empty *result list* that is the value of the expression
- For each element in the iterable value of <iter exp>:
 - Bind <name> to that element in the new frame from step 1
 - If <filter exp> evaluates to a true value, then add the value of <map exp> to the result list

Dictionaries:

```
words = {
    "más": "more",
    "otro": "other",
    "agua": "water"
}
>>> len(words)
3
>>> "agua" in words
True
>>> words["otro"]
'other'
>>> words["pavo"]
KeyError
>>> words.get("pavo", "🐔")
'🐔'
```

Dictionary comprehensions:

```
{key: value for <name> in <iter exp>}
>>> {x: x*x for x in range(3,6)}
{3: 9, 4: 16, 5: 25}
>>> [word for word in words]
['más', 'otro', 'agua']
>>> [words[word] for word in words]
['more', 'other', 'water']
>>> words["oruguita"] = 'caterpillar'
>>> words["oruguita"]
'caterpillar'
>>> words["oruguita"] += '🐛'
>>> words["oruguita"]
'caterpillar🐛'
```

Functions that aggregate iterable arguments

- `sum(iterable[, start])` -> value *sum of all values*
- `max(iterable[, key=func])` -> value *largest value*
- `max(a, b, c, ..., key=func)` -> value
- `min(iterable[, key=func])` -> value *smallest value*
- `min(a, b, c, ..., key=func)` -> value
- `all(iterable)` -> bool *whether all are true*
- `any(iterable)` -> bool *whether any is true*

Many built-in Python sequence operations return iterators that compute results lazily

- `map(func, iterable):` Iterate over func(x) for x in iterable
- `filter(func, iterable):` Iterate over x in iterable if func(x)
- `zip(first_iter, second_iter):` Iterate over co-indexed (x, y) pairs
- `reversed(sequence):` Iterate over x in a sequence in reverse order
- `list(iterable):` Create a list containing all x in iterable
- `tuple(iterable):` Create a tuple containing all x in iterable
- `sorted(iterable):` Create a sorted list containing x in iterable

To view the contents of an iterator, place the resulting elements into a container

```
def cascade(n):
    if n < 10:
        print(n)
    else:
        print(n)
        cascade(n//10)
        print(n)

>>> cascade(123)
123
12
1
123
12
1

def virfib(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return virfib(n-2) + virfib(n-1)

n: 0, 1, 2, 3, 4, 5, 6, 7, 8,
virfib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,
```

- Exponential growth.** E.g., recursive fib $\Theta(b^n)$ $O(b^n)$
Incrementing *n* multiplies *time* by a constant
- Quadratic growth.** E.g., overlap $\Theta(n^2)$ $O(n^2)$
Incrementing *n* increases *time* by *n* times a constant
- Linear growth.** E.g., slow exp $\Theta(n)$ $O(n)$
Incrementing *n* increases *time* by a constant
- Logarithmic growth.** E.g., exp_fast $\Theta(\log n)$ $O(\log n)$
Doubling *n* only increments *time* by a constant
- Constant growth.** Incrementing *n* doesn't affect time $\Theta(1)$ $O(1)$



List mutation:

```
>>> a = [10]
>>> b = a
>>> a == b
True
>>> a.append(20)
>>> a == b
True
>>> a
[10, 20]
>>> b
[10, 20]

>>> a = [10]
>>> b = [10]
>>> a == b
True
>>> b.append(20)
>>> a
[10]
>>> b
[10, 20]
>>> a == b
False
```

You can *copy* a list by calling the list constructor or slicing the list from the beginning to the end.

```
>>> a = [10, 20, 30]
>>> list(a)
[10, 20, 30]
>>> a[:]
[10, 20, 30]
```

Tuples:

```
>>> empty = ()
>>> len(empty)
0
>>> conditions = ('rain', 'shine')
>>> conditions[0]
'rain'
>>> conditions[0] = 'fog'
Error
```

```
>>> all([False, True])
False
>>> all([])
True
>>> sum([1, 2])
3
>>> sum([1, 2], 3)
6
>>> sum([])
0
>>> sum([[1], [2]], [])
[1, 2]

>>> any([False, True])
True
>>> any([])
False
>>> max([1, 2])
2
>>> max([1, 2])
2
>>> max([1, -2], key=abs)
-2
```

List methods:

```
>>> suits = ['coin', 'string', 'myriad']
>>> suits.pop()
'myriad'
>>> suits.remove('string')

>>> suits.append('cup')
>>> suits.extend(['sword', 'club'])
>>> suits[2] = 'spade'
>>> suits
['coin', 'cup', 'spade', 'club']
>>> suits[0:2] = ['diamond']
>>> suits
['diamond', 'spade', 'club']
>>> suits.insert(0, 'heart')
>>> suits
['heart', 'diamond', 'spade', 'club']
```

Remove and return the last element

Removes first matching value

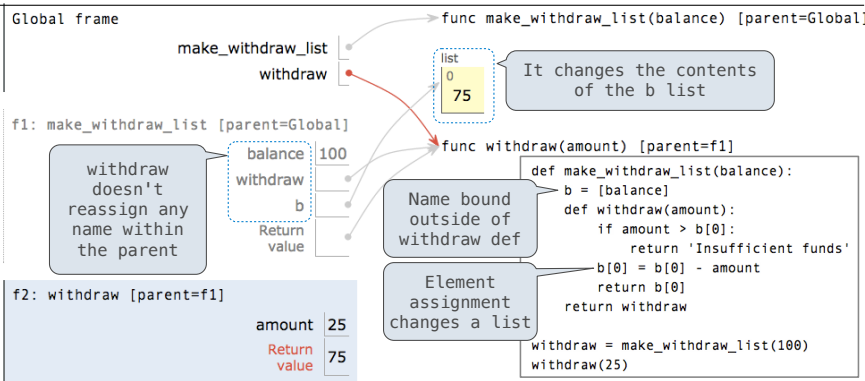
Add all values

Replace a slice with values

Add an element at an index

```
False values:
•Zero
•False
•None
•An empty string, list, dict, tuple
All other values are true values.

>>> bool(0)
False
>>> bool(1)
True
>>> bool('')
False
>>> bool('0')
True
>>> bool([])
False
>>> bool([[]])
True
>>> bool({})
False
>>> bool(())
False
>>> bool(lambda x: 0)
True
```



```
iter(iterable):
Return an iterator over the elements of an iterable value
next(iterator):
Return the next element

>>> s = [3, 4, 5]
>>> t = iter(s)
>>> next(t)
3
>>> next(t)
4

>>> d = {'one': 1, 'two': 2, 'three': 3}
>>> k = iter(d)
>>> next(k)
'one'
>>> next(k)
'two'
```

```
A generator function is a function that yields values instead of returning.
>>> def plus_minus(x):
...     yield x
...     yield -x
>>> t = plus_minus(3)
>>> next(t)
3
>>> next(t)
-3

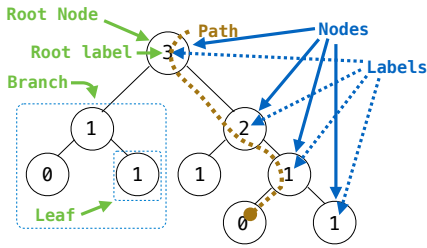
def a_then_b(a, b):
    yield from a
    yield from b
>>> list(a_then_b([3, 4], [5, 6]))
[3, 4, 5, 6]
```

Recursive description:

- A tree has a root label and a list of branches
- Each branch is a tree
- A tree with zero branches is called a leaf

Relative description:

- Each location is a node
- Each node has a label
- One node can be the parent/child of another



def tree(label, branches=[]):

```
for branch in branches:
    assert is_tree(branch)
return [label] + list(branches)
```

Verifies the tree definition

def label(tree):

```
return tree[0]
```

Creates a list from a sequence of branches

def branches(tree):

```
return tree[1:]
```

Verifies that tree is bound to a list

def is_tree(tree):

```
if type(tree) != list or len(tree) < 1:
    return False
for branch in branches(tree):
    if not is_tree(branch):
        return False
return True
```

def is_leaf(tree):

```
return not branches(tree)
```

def leaves(t):

```
if n == 0 or n == 1:
    return tree(n)
else:
    left = fib_tree(n-2)
    right = fib_tree(n-1)
    fib_n = label(left) + label(right)
    return tree(fib_n, [left, right])
```

```
>>> tree(3, [tree(1),
...         tree(2, [tree(1),
...                 tree(1)])])
[3, [1], [2, [1], [1]]]
```

def fib_tree(n):

```
if n == 0 or n == 1:
    return tree(n)
else:
    left = fib_tree(n-2)
    right = fib_tree(n-1)
    fib_n = label(left) + label(right)
    return tree(fib_n, [left, right])

return sum([leaves(b) for b in branches(t)], [])
```

class Tree:

```
def __init__(self, label, branches=[]):
    self.label = label
    for branch in branches:
        assert isinstance(branch, Tree)
    self.branches = list(branches)
```

Built-in isinstance function: returns True if branch has a class that is or inherits from Tree

def is_leaf(self):

```
return not self.branches
```

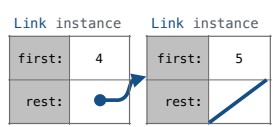
def leaves(tree):

```
"The leaf values in a tree."
if tree.is_leaf():
    return [tree.label]
else:
    return sum([leaves(b) for b in tree.branches], [])
```

class Link:

```
empty = ()
def __init__(self, first, rest=empty):
    self.first = first
    self.rest = rest
```

Some zero length sequence



def __repr__(self):

```
if self.rest:
    rest = ', ' + repr(self.rest)
else:
    rest = ''
return 'Link(' + repr(self.first) + rest + ')'
```

def __str__(self):

```
string = '<'
while self.rest is not Link.empty:
    string += str(self.first) + ' '
    self = self.rest
return string + str(self.first) + '>'
```

Anatomy of a recursive function:

- The def statement header is like any function
- Conditional statements check for base cases
- Base cases are evaluated without recursive calls
- Recursive cases are evaluated with recursive calls

```
def sum_digits(n):
    """Sum the digits of positive integer n."""
    if n < 10:
        return n
    else:
        all_but_last, last = n // 10, n % 10
        return sum_digits(all_but_last) + last
```

Recursive decomposition: finding simpler instances of a problem.

- E.g., count_partitions(6, 4)
- Explore two possibilities:
 - Use at least one 4
 - Don't use any 4
- Solve two simpler problems:
 - count_partitions(2, 4)
 - count_partitions(6, 3)
- Tree recursion often involves exploring different choices.

```
def count_partitions(n, m):
    if n == 0:
        return 1
    elif n < 0:
        return 0
    elif m == 0:
        return 0
    else:
        with_m = count_partitions(n-m, m)
        without_m = count_partitions(n, m-1)
        return with_m + without_m
```

Python object system:

Idea: All bank accounts have a balance and an account holder; the Account class should add those attributes to each of its instances

```
>>> a = Account('Jim')
>>> a.holder
'Jim'
>>> a.balance
0
```

An account instance
balance: 0 holder: 'Jim'

When a class is called:

1. A new instance of that class is created:
2. The `__init__` method of the class is called with the new object as its first argument (named `self`), along with any additional arguments provided in the call expression.

class Account:

```
def __init__(self, account_holder):
    self.balance = 0
    self.holder = account_holder
def deposit(self, amount):
    self.balance = self.balance + amount
    return self.balance
def withdraw(self, amount):
    if amount > self.balance:
        return 'Insufficient funds'
    self.balance = self.balance - amount
    return self.balance
```

`__init__` is called a constructor

`self` should always be bound to an instance of the Account class or a subclass of Account

Function call: all arguments within parentheses

```
>>> type(Account.deposit)
<class 'function'>
>>> type(a.deposit)
<class 'method'>
```

Method invocation: One object before the dot and other arguments within parentheses

```
>>> Account.deposit(a, 5)
```

```
10
>>> a.deposit(2)
12
```

Call expression

Dot expression

<expression> . <name>

The <expression> can be any valid Python expression.

The <name> must be a simple name.

Evaluates to the value of the attribute looked up by <name> in the object that is the value of the <expression>.

To evaluate a dot expression:

1. Evaluate the <expression> to the left of the dot, which yields the object of the dot expression
2. <name> is matched against the instance attributes of that object; if an attribute with that name exists, its value is returned
3. If not, <name> is looked up in the class, which yields a class attribute value
4. That value is returned unless it is a function, in which case a bound method is returned instead

Assignment statements with a dot expression on their left-hand side affect attributes for the object of that dot expression

- If the object is an instance, then assignment sets an instance attribute
- If the object is a class, then assignment sets a class attribute

Account class attributes

```
interest: 0.02 0.04 0.05
(withdraw, deposit, __init__)
```

Instance attributes of jim_account

```
balance: 0
holder: 'Jim'
interest: 0.08
```

Instance attributes of tom_account

```
balance: 0
holder: 'Tom'
```

```
>>> jim_account = Account('Jim')
>>> tom_account = Account('Tom')
>>> tom_account.interest
0.02
>>> jim_account.interest
0.02
>>> Account.interest = 0.04
>>> tom_account.interest
0.04
>>> jim_account.interest
0.04
```

class CheckingAccount(Account):

```
"""A bank account that charges for withdrawals."""
withdraw_fee = 1
interest = 0.01
def withdraw(self, amount):
    return Account.withdraw(self, amount + self.withdraw_fee)
    or
    return super().withdraw(amount + self.withdraw_fee)
```

To look up a name in a class:

1. If it names an attribute in the class, return the attribute value.
2. Otherwise, look up the name in the base class, if there is one.

```
>>> ch = CheckingAccount('Tom') # Calls Account.__init__
>>> ch.interest # Found in CheckingAccount
0.01
>>> ch.deposit(20) # Found in Account
20
>>> ch.withdraw(5) # Found in CheckingAccount
14
```