

**Import statement**

```
1 from math import pi
2 tau = 2 * pi
```

**Assignment statement**

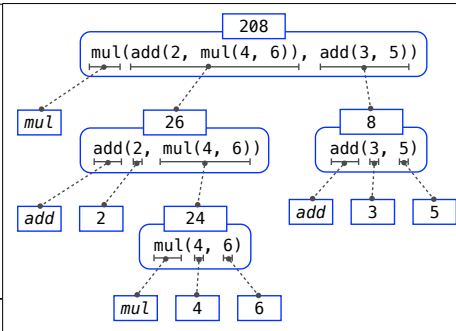
**Global frame**

Name	Value
pi	3.1416

**Binding**

**Code (left):** Statements and expressions  
Red arrow points to next line. Gray arrow points to the line just executed

**Frames (right):** A name is bound to a value  
In a frame, there is at most one binding per name



**Pure Functions**

```
-2 abs(number): 2
2, 10 pow(x, y): 1024
```

**Non-Pure Functions**

```
-2 print(...): None
```

display "-2"

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(-2)
```

**Built-in function**

mul

**User-defined function**

square

**Global frame**

Name	Value
mul	func mul(...)
square	func square(x)

**Local frame**

Name	Value
f1: square	[parent=Global]
x	-2
Return value	4

Return value is not a binding!

**Defining:**

```
>>> def square(x):
    return mul(x, x)
```

**Def statement:** Formal parameter (x), Return expression (return mul(x, x)), Body (return statement)

**Call expression:** square(2+2) operand: 2+2 argument: 4

operator: square  
function: func square(x)

```
1 def strconcat(a, b):
2     print(a + " " + b)
3
4 strconcat("hello", "world")
```

hello world

**A and B:**  
True if A is True and B is True  
**A or B:**  
True if A is True or B is True  
**not A:**  
True if A is False  
False if A is True

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(square(3))
```

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

**Global frame**

Name	Value
mul	func mul(...)
square	func square(x)

**Local frame**

Name	Value
f1: square	[parent=Global]
x	3
Return value	9

**Local frame**

Name	Value
f2: square	[parent=Global]
x	9
Return value	81

**Calling/Applying:** square(x): Argument (x), Intrinsic name (square), Return value (mul(x, x))

```
def abs_value(x):
    if x > 0:
        return x
    elif x == 0:
        return 0
    else:
        return -x
```

1 statement, 3 clauses, 3 headers, 3 suites, 2 boolean contexts

**Evaluation rule for call expressions:**

- Evaluate the operator and operand subexpressions.
- Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions.

**Applying user-defined functions:**

- Create a new local frame with the same parent as the function that was applied.
- Bind the arguments to the function's formal parameter names in that frame.
- Execute the body of the function in the environment beginning at that frame.

```
1 def f(x, y):
2     return g(x)
3
4 def g(a):
5     return a + y
6
7 result = f(1, 2)
```

**Global frame**

Name	Value
f1: f	[parent=Global]
x	1
y	2
f2: g	[parent=Global]
a	1

Error: "y" is not found

- An environment is a sequence of frames
- An environment for a non-nested function (no def within def) consists of one local frame, followed by the global frame

**Execution rule for def statements:**

- Create a new function value with the specified name, formal parameters, and function body.
- Its parent is the first frame of the current environment.
- Bind the name of the function to the function value in the first frame of the current environment.

**Execution rule for assignment statements:**

- Evaluate the expression(s) on the right of the equal sign.
- Simultaneously bind the names on the left to those values, in the first frame of the current environment.

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(4)
```

**Global frame**

Name	Value
mul	func mul(...)
square	func square(x)

**Local frame**

Name	Value
f1: square	[parent=Global]
square	4
Return value	16

A call expression and the body of the function being called are evaluated in different environments

**Higher-order function:** A function that takes a function as an argument value or returns a function as a return value

**Nested def statements:** Functions defined within other function bodies are bound to names in the local frame

**Execution rule for conditional statements:** Each clause is considered in order.

- Evaluate the header's expression.
- If it is a true value, execute the suite, then skip the remaining clauses in the statement.

**Evaluation rule for or expressions:**

- Evaluate the subexpression <left>.
- If the result is a true value v, then the expression evaluates to v.
- Otherwise, the expression evaluates to the value of the subexpression <right>.

**Evaluation rule for and expressions:**

- Evaluate the subexpression <left>.
- If the result is a false value v, then the expression evaluates to v.
- Otherwise, the expression evaluates to the value of the subexpression <right>.

**Evaluation rule for not expressions:**

- Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

**Execution rule for while statements:**

- Evaluate the header's expression.
- If it is a true value, execute the (whole) suite, then return to step 1.

```
def fib(n):
    """Compute the nth Fibonacci number, for N >= 1."""
    pred, curr = 0, 1 # Zeroth and first Fibonacci numbers
    k = 1 # curr is the kth Fibonacci number
    while k < n:
        pred, curr = curr, pred + curr
        k = k + 1
    return curr
```

```
def cube(k):
    return pow(k, 3)
```

```
def summation(n, term):
    """Sum the first n terms of a sequence.

    >>> summation(5, cube)
    225
    """
    total, k = 0, 1
    while k <= n:
        total, k = total + term(k), k + 1
    return total
```

0 + 1<sup>3</sup> + 2<sup>3</sup> + 3<sup>3</sup> + 4<sup>3</sup> + 5<sup>3</sup>

Function of a single argument (not called term)

A formal parameter that will be bound to a function

The cube function is passed as an argument value

The function bound to term gets called here

